

# Electrical Properties of Neurons

Chapter 4

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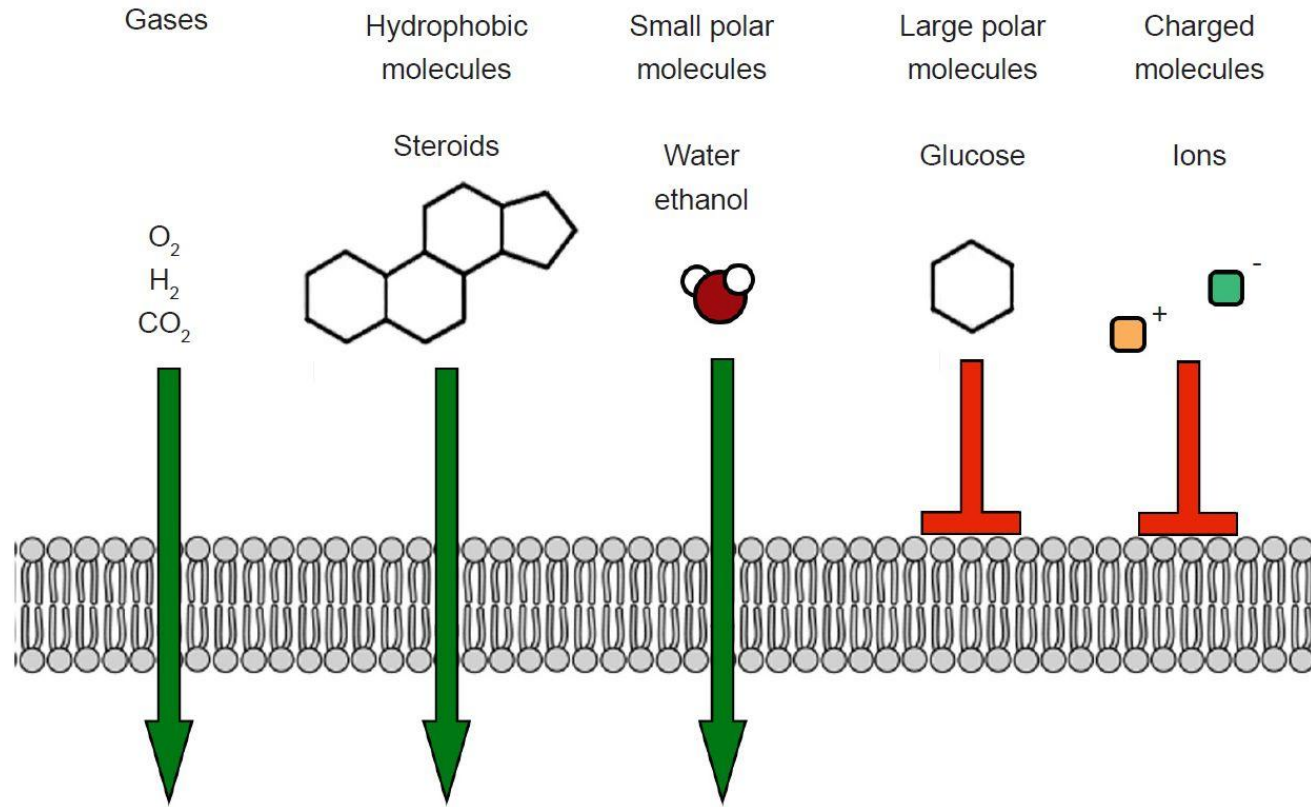
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# Ion channels - Membrane

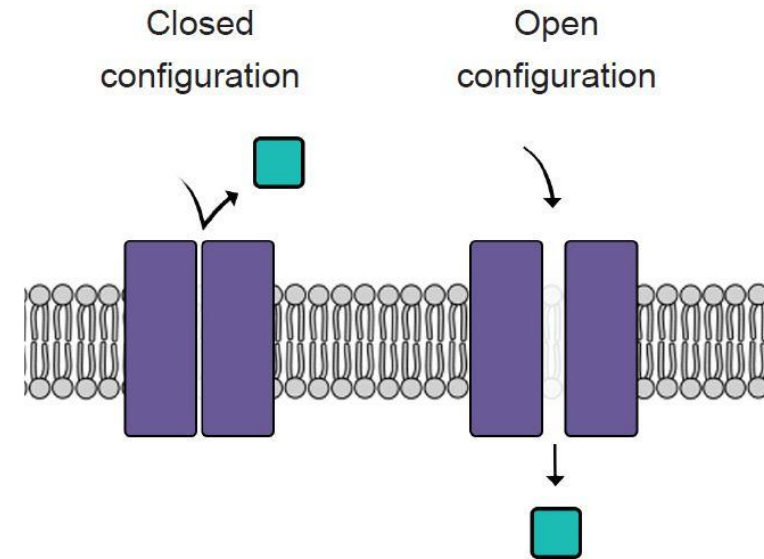
- Selectively permeable membrane of cell
  - Gases and water molecules can pass easily
  - Large molecules (ex. glucose) and charged molecules like ions or amino acids are unable



**Figure 4.1** Selective permeability of molecules across the cell membrane.

# Ion channels

- Transmembrane proteins have pores that are like "tunnels" allowing molecules and ions to pass
- Called ion channels
- Channels are passive (no cellular energy is required to move ions)
- Special molecular characteristics allow specific ions to pass and exclude other ions



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**Figure 4.2** Ion channels (purple) are transmembrane proteins that can be open, allowing charged ions to cross the cell membrane through a molecular “tunnel” called the pore.

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# Ion channel features to allow different ions to pass through:

## 1. Pore size

- Only ions of a diameter equal to or less than the diameter of the ion channel can pass through
- Excludes larger diameter ions

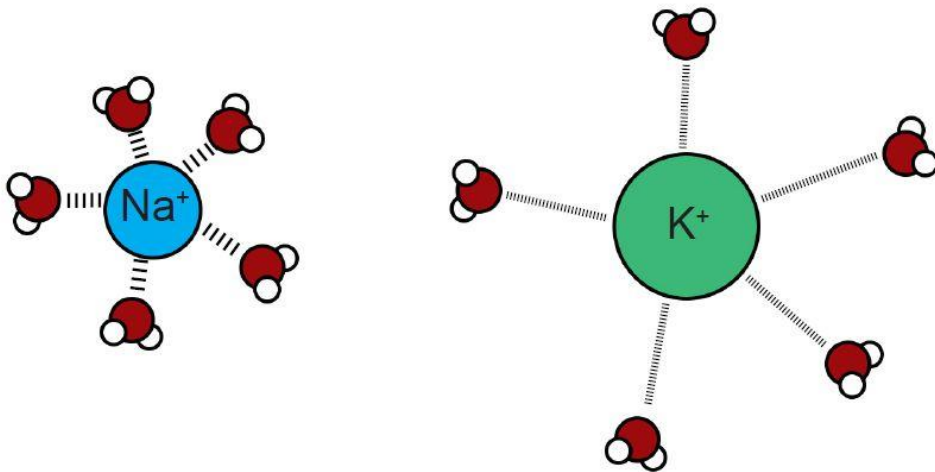
## 2. Electrical charge

- Charged amino acids line the inside of the pore
- Their charge allows only certain ions to pass
  - Like charges repel and opposites attract

## 3. Hydration shell

- Water molecules around an ion forms a “hydration shell”
- Ion channel selectivity is derived from the
  - hydration shell radius
  - number of water molecules
  - orientation of water molecules

# Hydration shell example



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**Figure 4.3** Ions dissolved in water are surrounded by a shell of water molecules. The potassium ion is larger, and the water molecules are farther apart, making the attraction weaker than in the sodium ion.

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- $\text{K}^+$  and  $\text{Na}^+$  are both too big to pass through  $\text{K}^+$  channel with their hydration shells intact
- $\text{K}^+$  easily loses a water molecule from its hydration shell
  - It then fits through the channel
  - In addition,  $\text{K}^+$  is large enough to interact with amino acids lining the inside of the channel to facilitate its movement through
- It is harder (takes more energy) for  $\text{Na}^+$  to lose a water molecule
  - Therefore, it is not “energetically favourable” for the  $\text{Na}^+$  to pass through
  - Even when  $\text{Na}^+$  does lose a water molecule, it is too small to interact with the amino acids lining the inside of the channel

# Classes of ion channels

- Leak channels
  - Persistently open
  - Ex. Potassium ( $K^+$ ) and chloride ( $Cl^-$ ) leak channels
  - Movement depends solely on **electrochemical gradient** (next slide)
- Voltage-gated ion channels
  - Sensitive to the electrical potential of the surrounding membrane
  - Many remain closed at negative potentials (resting condition) and open at positive potentials (action potential)
- Ligand-gated ion channels (AKA ionotropic receptors)
  - Open in response to binding certain molecules
- Catch-all category of ion channels used by the sensory systems
  - Open and close in response to unique stimuli depending on what they are able to sense (hair cells in ears, Pacinian corpuscles in skin, Golgi tendon organ in muscles, and ion channels of photoreceptors in eyes)

# The electrochemical gradient

- Movement of ions across channel depend on channel being present and open AND specific conditions inside and outside of cell
- Once open, two forces act on ions:
  1. Electrical gradient
  2. Chemical gradient
- Together these forces are known as the electrochemical gradient
- To predict forces acting on ion, need to know
  1. Charge of ion
  2. Relative concentrations of ions across membrane

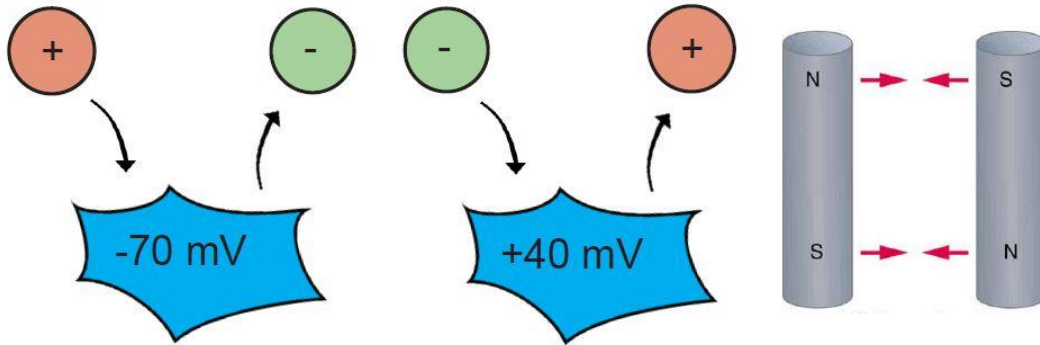


# Electrical gradient

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**Figure 4.4** The electrical gradient describes the forces acting on ions as they follow the rules of magnetism in physics - “opposites attract, and similar charges repel.”

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- Refers to electrical forces acting on charged molecules (pull opposite charges together; push like charges away)
- At rest, interior of cell has negative charge (about -70 mV)
  - Positive charges are attracted while negative charges are repelled
- As neuron's membrane potential ( $V_m$ ) changes (e.g., to +40 mV), the force exerted by electrical gradient also changes

# Chemical gradient



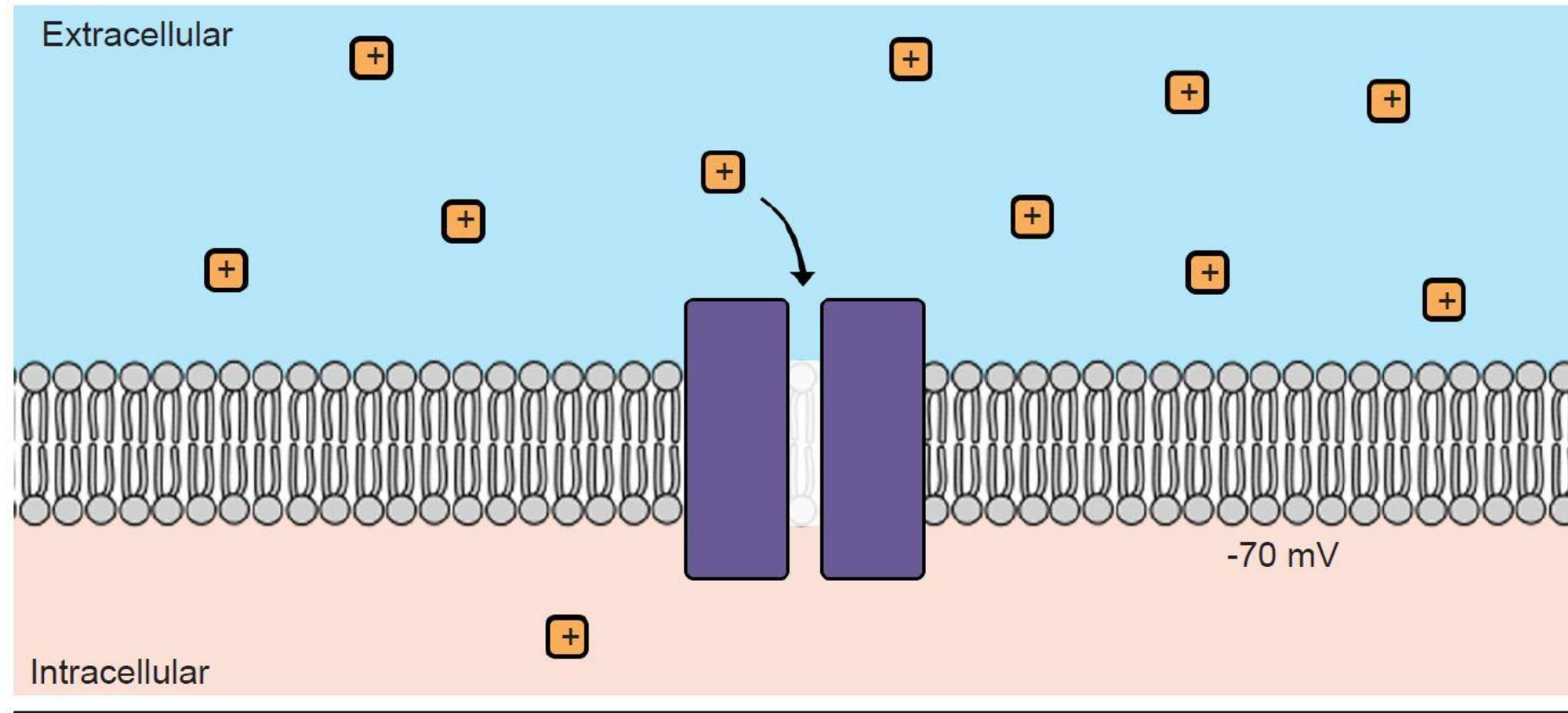
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**Figure 4.5** The chemical gradient describes the same forces acting on ions as diffusion, where ions move from areas of high concentration to low concentration.

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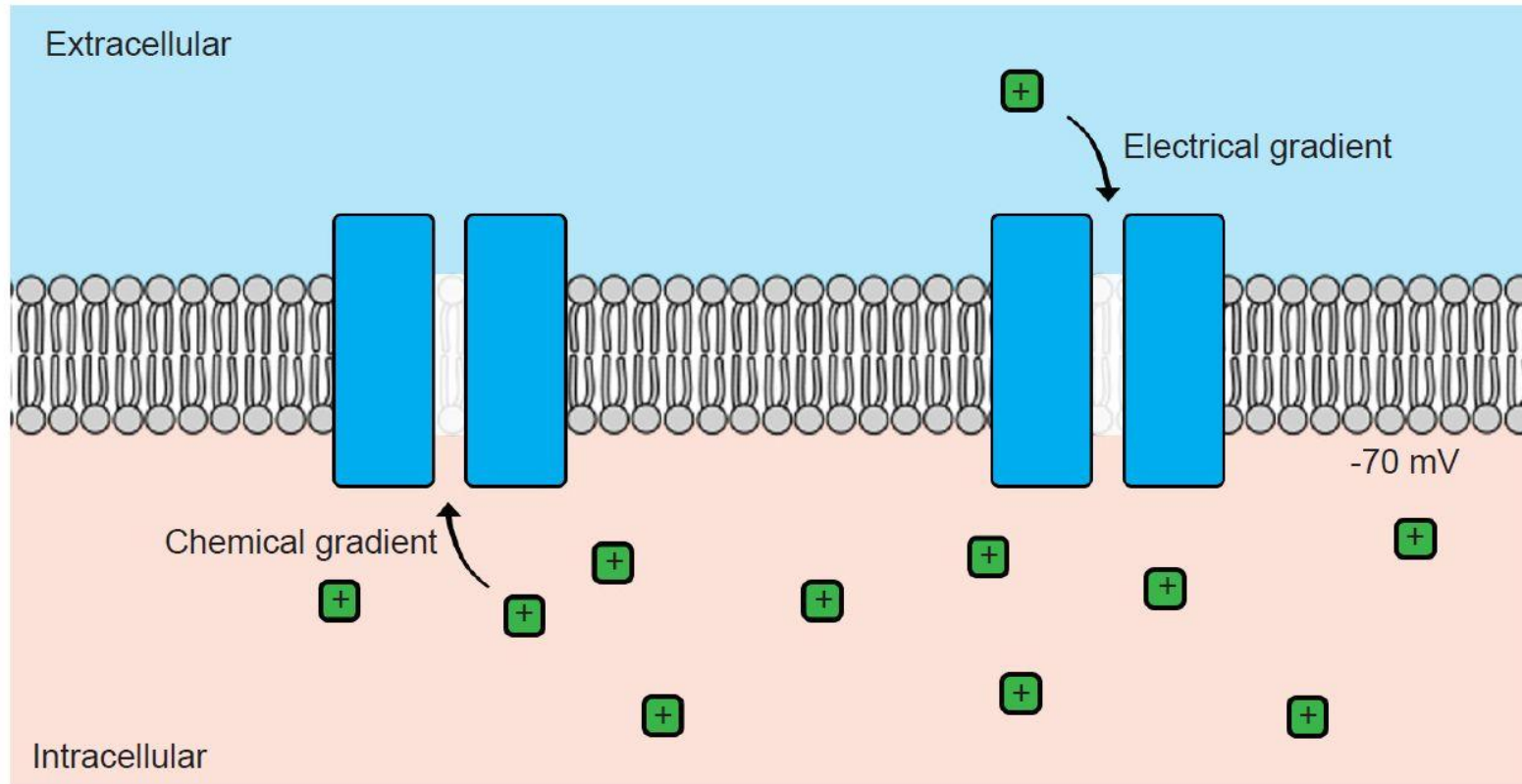
- Natural process by which high concentration of substance will eventually diffuse to lower concentration and settle evenly over space
- Unaffected by biological movement of ions

# Net flow into the cell



**Figure 4.6** When a sodium channel opens (purple), sodium ions (orange) are acted on by two forces. They have a positive charge, which is attracted to the negatively-charged inside of the cell (electrical gradient). They are at a higher concentration outside the cell, which causes them to move to the inside of the cell with the lower concentration (chemical gradient).

# Dynamic equilibrium



**Figure 4.7** When a potassium channel opens (blue), potassium ions (green) are acted on by two opposing forces. They have a positive charge, which is attracted to the negatively-charged inside of the cell (electrical gradient). At the same time, they are at a higher concentration inside the cell, which causes them to want to move outside of the cell (chemical gradient). This process is at equilibrium.

# More on dynamic equilibrium

- Dynamic, because constant movement of ions **but**
- Equilibrium, because no net movement of charge
- Exact value of  $V_m$  is called equilibrium potential for the ion (abbreviated as  $E_x$ , where x is ion of interest)
- $E_x$  differs for each ion

# Ion concentrations

| Ion                  | Abbreviation     | Concentration outside $[X]_o$ | Concentration inside $[X]_i$ |
|----------------------|------------------|-------------------------------|------------------------------|
| Sodium               | $\text{Na}^+$    | 140 mM                        | 15 mM                        |
| Potassium            | $\text{K}^+$     | 5 mM                          | 150 mM                       |
| Chloride             | $\text{Cl}^-$    | 120 mM                        | 10 mM                        |
| Calcium              | $\text{Ca}^{2+}$ | 1 mM                          | 100 nM = 0.1 $\mu\text{M}$   |
| Magnesium            | $\text{Mg}^{2+}$ | 2 mM                          | 0.5 mM                       |
| Miscellaneous anions | $\text{A}^-$     | 20 mM                         | 100 mM                       |

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**Table 4.8** Charged ions are unequally distributed across the cell membrane. Typical concentrations of ions in a mammalian neuron.

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# The Nernst equation

- Possible to calculate equilibrium potential ( $E_x$ ) for each ion
- Use Nernst equation
- $E_x$  = equilibrium potential (usually measured in mV)
- $E_x$  is AKA reversal potential and Nernst potential
  - Voltage at which the net movement of the ion (i.e., into the cell, out of the cell) reverses direction

# Meaning of equation elements

$$E_x = \frac{RT}{zF} \ln \left( \frac{[x]_o}{[x]_i} \right)$$

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**Equation 4.9** The Nernst equation calculates the reversal potential for a given ion x.

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- $E_x$  = equilibrium potential (usually measured in mV)
- $R$  = ideal gas constant = 8.314 J/K\*mol
- $T$  = temperature in Kelvin (about 310K for biological temps)
- $z$  = electrical charge of ion
- $F$  = Faraday constant = 96,485 Coulombs/mol
- $[x]_o$  and  $[x]_i$  = concentration of ions outside and inside of cell, respectively



# Back-of-the-envelope equation

- Shortcut that condenses R and F constants and turns natural log into a base 10 logarithm and assumes physiological temperature

$$E_x \cong \frac{61}{z} \log \left( \frac{[x]_o}{[x]_i} \right)$$

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**Equation 4.10** The “back-of-the-envelope” equation is a shortcut to estimate the reversal potential for an ion x.

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# Example

- Calculate the equilibrium potential for calcium ions

# Mathematical explanation of movement

- Nernst equation is useful for calculating reversal potential for individual ions assuming the appropriate ion channels are open
- However, not all ion channels are opened or closed at the same time
- Goldman-Hodgkin-Katz equation combines the Nernst potentials for three relevant ions ( $\text{Na}^+$ ,  $\text{K}^+$ , and  $\text{Cl}^-$ )

# Goldman-Hodgkin-Katz (GHK) Equation

$$V_m = \frac{RT}{F} \ln \frac{p_K[K^+]_o + p_{Na}[Na^+]_o + p_{Cl}[Cl^-]_i}{p_K[K^+]_i + p_{Na}[Na^+]_i + p_{Cl}[Cl^-]_o}$$

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**Equation 4.11** The Goldman-Hodgkin-Katz equation is used to calculate the membrane potential given permeability of ions and their concentrations across the cell membrane.

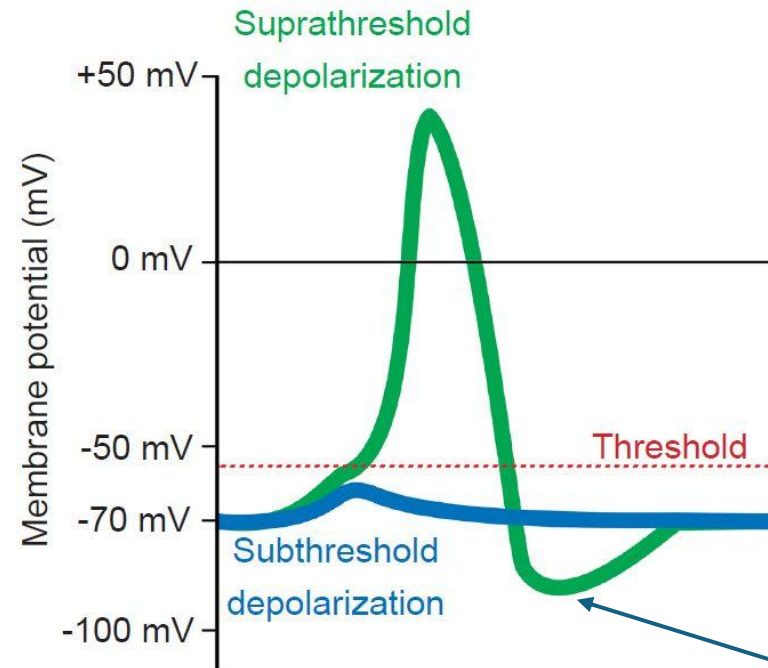
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- Combination of Nernst equations for equilibrium potentials for all 3 ions
- Introduces value of p (permeability)
  - Ability for ion to cross the membrane through ion channels
  - No units
- Higher the permeability of a given ion, closer the  $V_m$  to the  $E_x$  for that ion

# The action potential

- Short-lasting change (1 or 2 milliseconds) in membrane potential
- Triggers release of neurotransmitters at axon terminal of a chemical synapse
- All-or-nothing response
  - Sub-threshold changes in  $V_m$  are called graded potentials
- $V_m$  goes from negative to a more positive potential = depolarization
- Action potential threshold =  $\sim -55$  mV
- Change in membrane potential is due to movement of ions, especially  $\text{Na}^+$  and  $\text{K}^+$  through voltage-gated ion channels

# Characteristic "shape" of action potential



**Figure 4.13** If the depolarization exceeds the action potential threshold, roughly -55 mV, the neuron will fire an action potential (green).

hyperpolarization

# Steps of action potential

1. Depolarization from incoming (input) neurons
2. Opening of voltage-gated  $\text{Na}^+$  channels
3. Opening of voltage-gated  $\text{K}^+$  channels
4. Inactivation of voltage-gated  $\text{Na}^+$  channels
5. Deactivation of voltage-gated  $\text{K}^+$  channels

Some steps may overlap during action potential

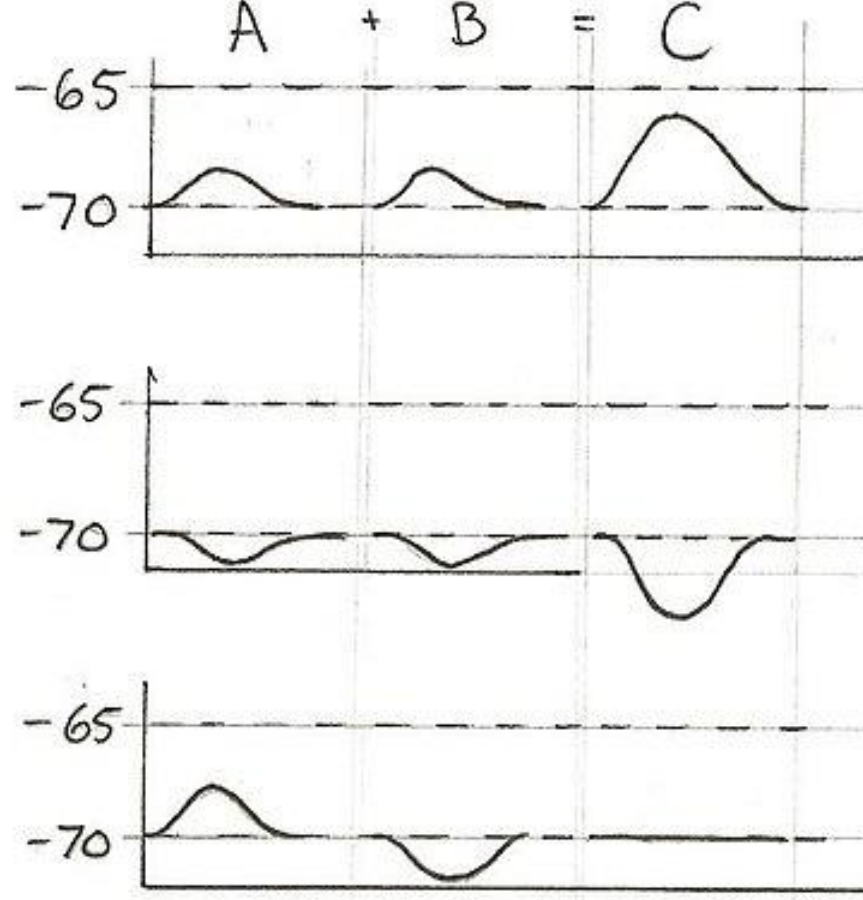
# Step 1: Depolarization from incoming neurons

- Presynaptic neurons release neurotransmitters causing some ion movement via postsynaptic ligand-gated ion channels
- Small deviations in membrane voltage = postsynaptic potentials (PSPs)
- Release of excitatory neurotransmitters leads to excitatory PSPs (EPSPs) – depolarizations (negative to less negative  $V_m$ )
- Release of inhibitory neurotransmitters leads to inhibitory PSPs (IPSPs) – hyperpolarizations (negative to more negative  $V_m$ )
- Often multiple EPSPs are required to bring  $V_m$  above threshold potential

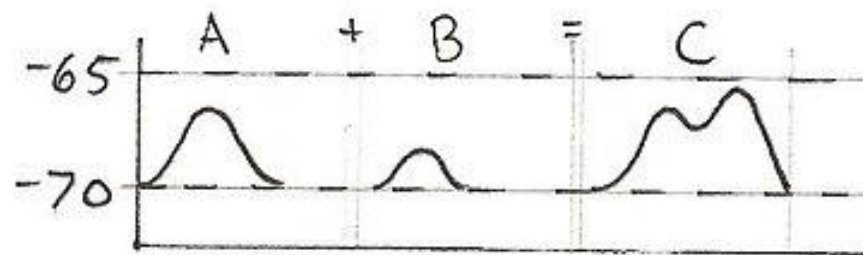


# Summation of EPSPs

- Spatial summation
  - Two EPSPs from two adjacent inputs are triggered
- Temporal summation
  - Multiple EPSPs from same input occur close together in time
  - Adding a second EPSP during decay period may allow a large enough change in  $V_m$  to reach threshold
- When large enough total depolarization of membrane potential reaches soma, action potential is initiated at axon hillock



• Examples of spatial summation.

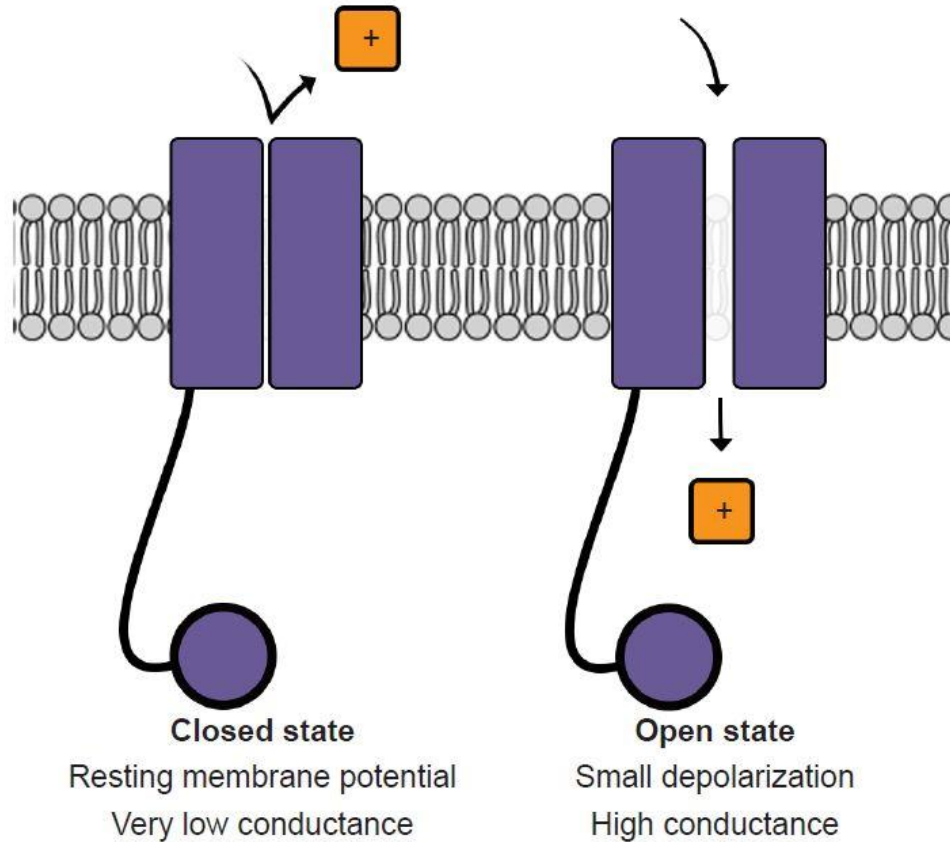


• An example of temporal summation

## Step 2: Opening of voltage-gated $\text{Na}^+$ channels

- At rest, voltage-gated ion channels are almost all closed
- As  $V_m$  depolarizes, channels are more likely to open
- Electrochemical gradient allows us to predict movement of  $\text{Na}^+$  ions
  - Positively charged sodium ions are drawn to negative inside
  - Ions move from area of high concentration (outside cell) to area of lower concentration (inside cell)
- Movement of  $\text{Na}^+$  into cell causes  $V_m$  to depolarize to very positive potential
  - Peak of action potential can reach +40 mV

# Voltage-gated $\text{Na}^+$ channels



**Figure 4.16** Voltage-gated  $\text{Na}^+$  channels have a molecular structure that allows the channel to temporarily change structure in response to membrane voltage. A small depolarization to  $-50$  mV causes the channels to open, while a large depolarization above  $-30$  mV causes the channels to inactivate, blocking further sodium currents.

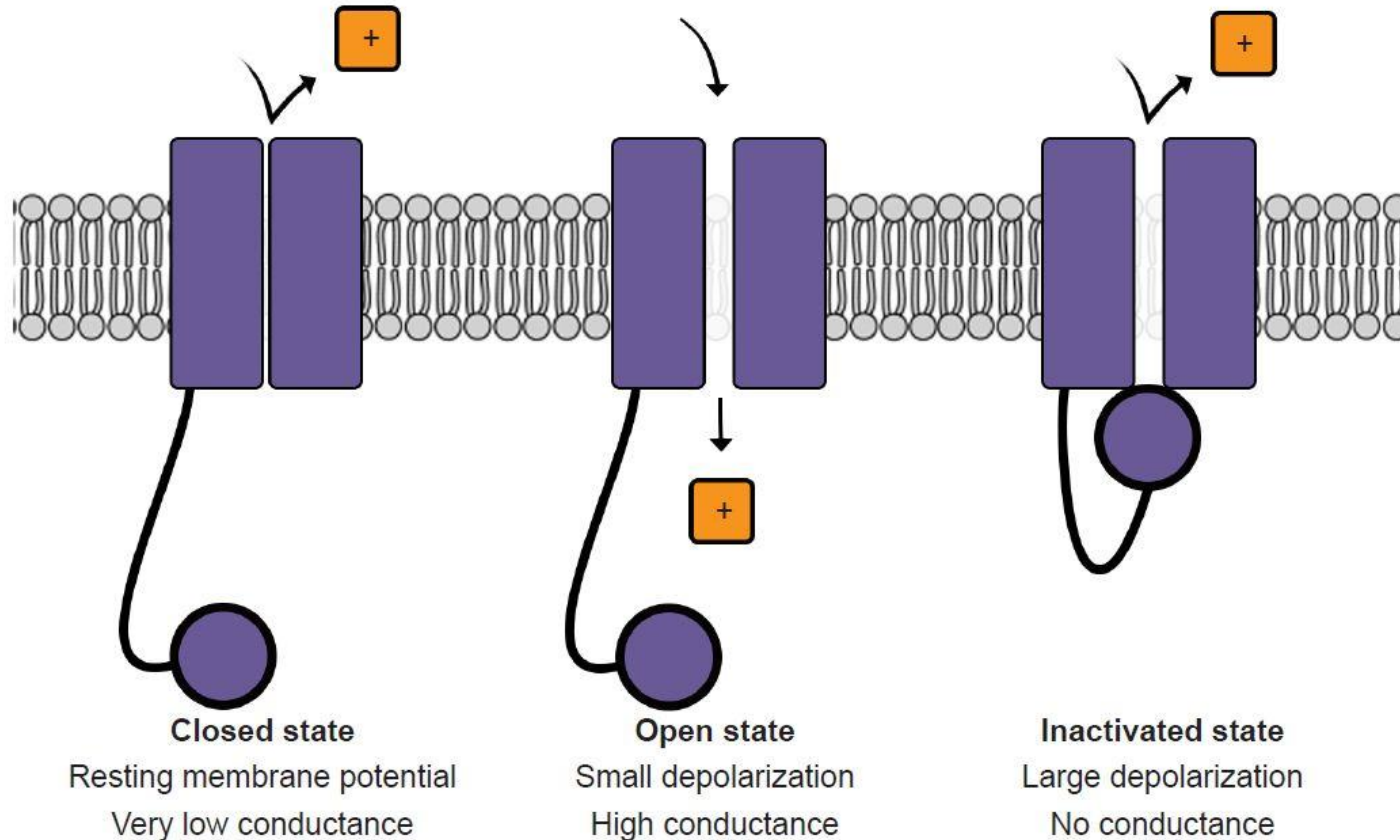
## Step 3: Opening of voltage-gated $K^+$ channels

- Like voltage-gated  $Na^+$  channels, these  $K^+$  channels open when cell starts to depolarize, allowing  $K^+$  ions the move across cell membrane
- Again, knowledge of electrochemical gradient can be applied
  - Positive potential inside neuron repels  $K^+$  ions
  - Relatively high concentration of  $K^+$  inside pushes  $K^+$  outside
- Interior of cell (and  $V_m$ ) become more negative
- Cells become more negative than the resting membrane potential

## Step 4: Inactivation of voltage-gated Na<sup>+</sup> channels

- In addition to the pore, these channels have inactivation gates
- When positive potential is reached, inactivation gate closes, preventing further movement of excitatory, depolarizing Na<sup>+</sup> ions
- Inactivation process is often faster than a millisecond

# Voltage-gated $\text{Na}^+$ channels

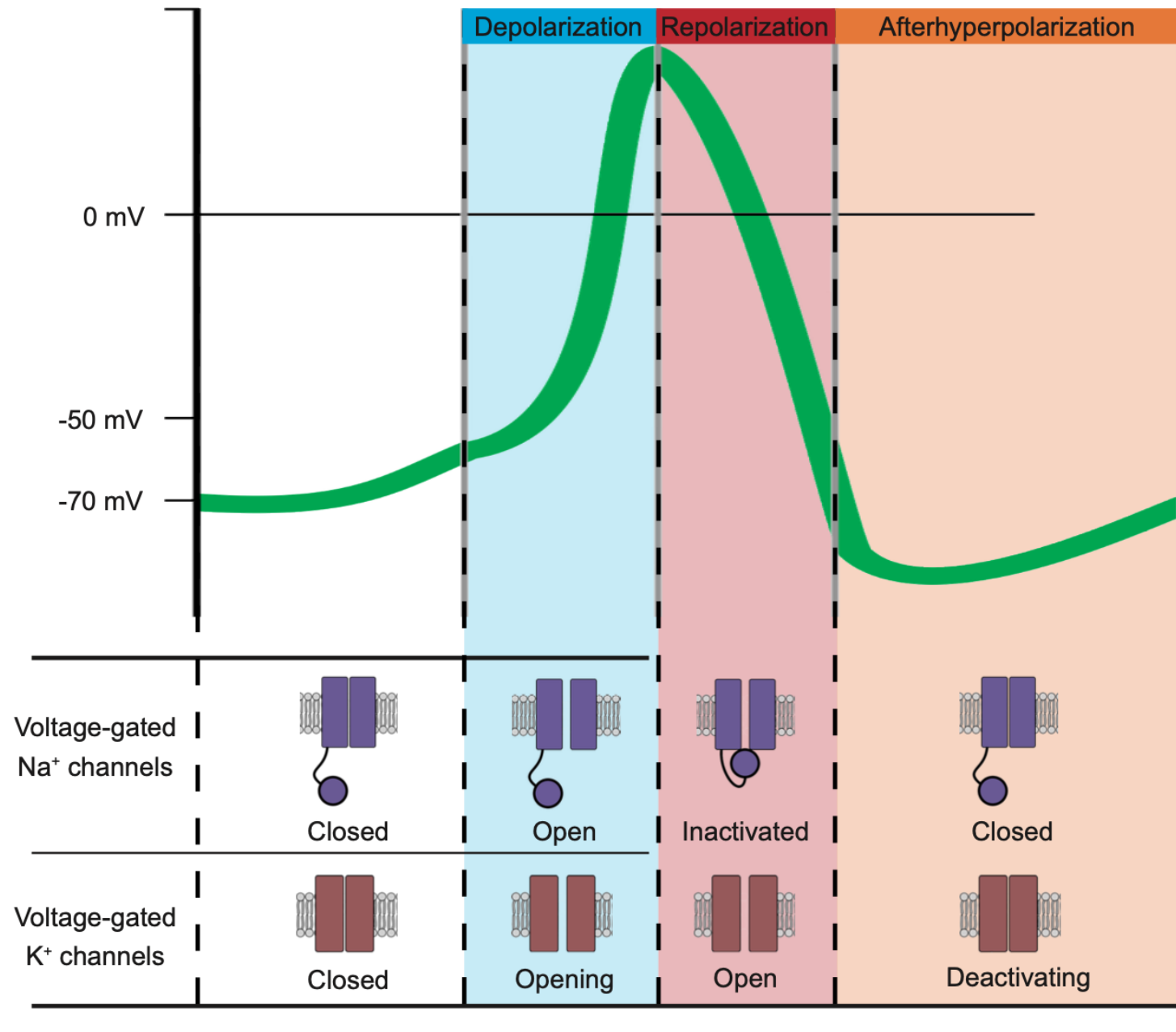


**Figure 4.16** Voltage-gated  $\text{Na}^+$  channels have a molecular structure that allows the channel to temporarily change structure in response to membrane voltage. A small depolarization to  $-50$  mV causes the channels to open, while a large depolarization above  $-30$  mV causes the channels to inactivate, blocking further sodium currents.

## Step 5: Deactivation of voltage-gated $K^+$ channels

- Main current flow is outward as  $K^+$  ions are driven out of cell through voltage-gated  $K^+$  channels by electrochemical gradient
- Interior once again becomes more negative
- Deactivation of voltage-gated  $K^+$  channels is much slower (a few milliseconds) than inactivation of  $Na^+$  channels
- Hyperpolarizing current stops, which causes membrane potential to gradually return to the resting potential





**Figure 4.17** Voltage-gated ion channels open, inactivate, and deactivate at different times during the action potential.

# Depolarization

- -70 mV to +40 mV (upward deflection of action potential)
- Lasts for 0.5 millisecond
- $V_m$  becomes more positive because  $\text{Na}^+$  enters cell through voltage-gated  $\text{Na}^+$  channels (Step 2)
- Voltage-gated  $\text{K}^+$  channels start to open (Step 3)

# Repolarization

- +40 mV to -70 mV (rapid downwards deflection)
- Also lasts ~0.5 milliseconds
- Voltage-gated  $\text{Na}^+$  channels have almost all inactivated (Step 4)
- $\text{K}^+$  are being drive out of the cell through voltage-gated potassium channels
- $V_m$  becomes more negative

# Afterhyperpolarization

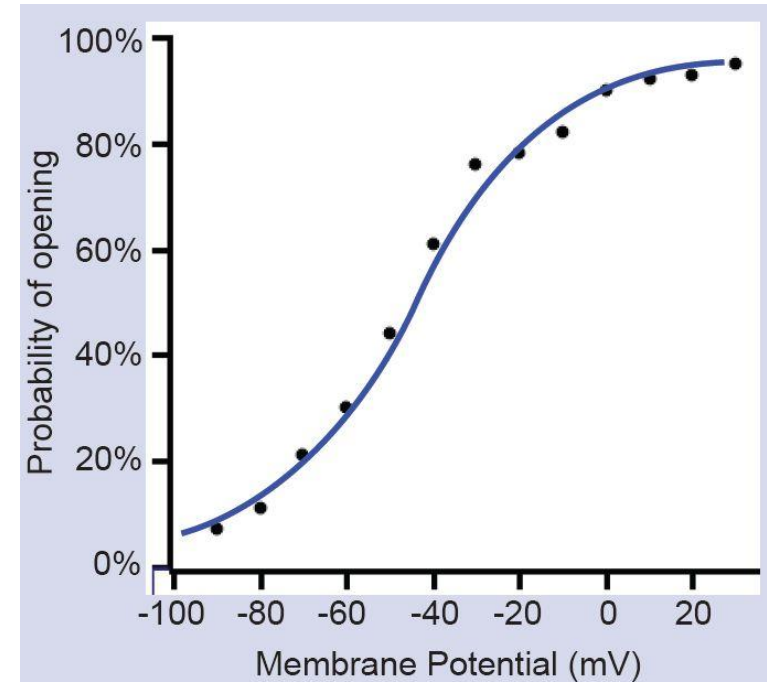
- -70 mV to -80 mV and back to -70 mV (slow return to resting membrane potential)
- Can last for a few milliseconds
- Gradual deactivation of voltage-gated K<sup>+</sup> channels (Step 5)

# Clinical connection: Chronic pain

- Nociception = sensory system's process of encoding noxious stimuli
- Pain = perception that the body is experiencing injury or noxious stimulus
- Pain triggers a reflex to withdraw from stimulus to decrease severity of damage and/or creates memories to discourage future contact with pain-inducing situations
  - A healthy, protective sensation
- Dysregulation of somatosensory system can cause people to experience pain even in the absence of injurious stimuli, a condition called allodynia
- Allodynia is not completely understood, but linked to change in voltage-gated  $\text{Na}^+$  channel properties that cause increase of excitability of pain-sensing neurons
- Not all chronic pain is allodynia

# Randomness in ion channel properties

- Voltage-gated ion channels do not follow "if-then" precision
- More probabilistic in nature
  - At  $-70$  mV, 0.1% chance to open
  - At  $-30$  mV, 50% chance to open
  - At  $+20$  mV, 99.9% chance to open



**Figure 4.18** Opening of voltage-gated ion channels is probabilistic, with a greater likelihood of opening at depolarized potentials.

# Changes in $V_m$

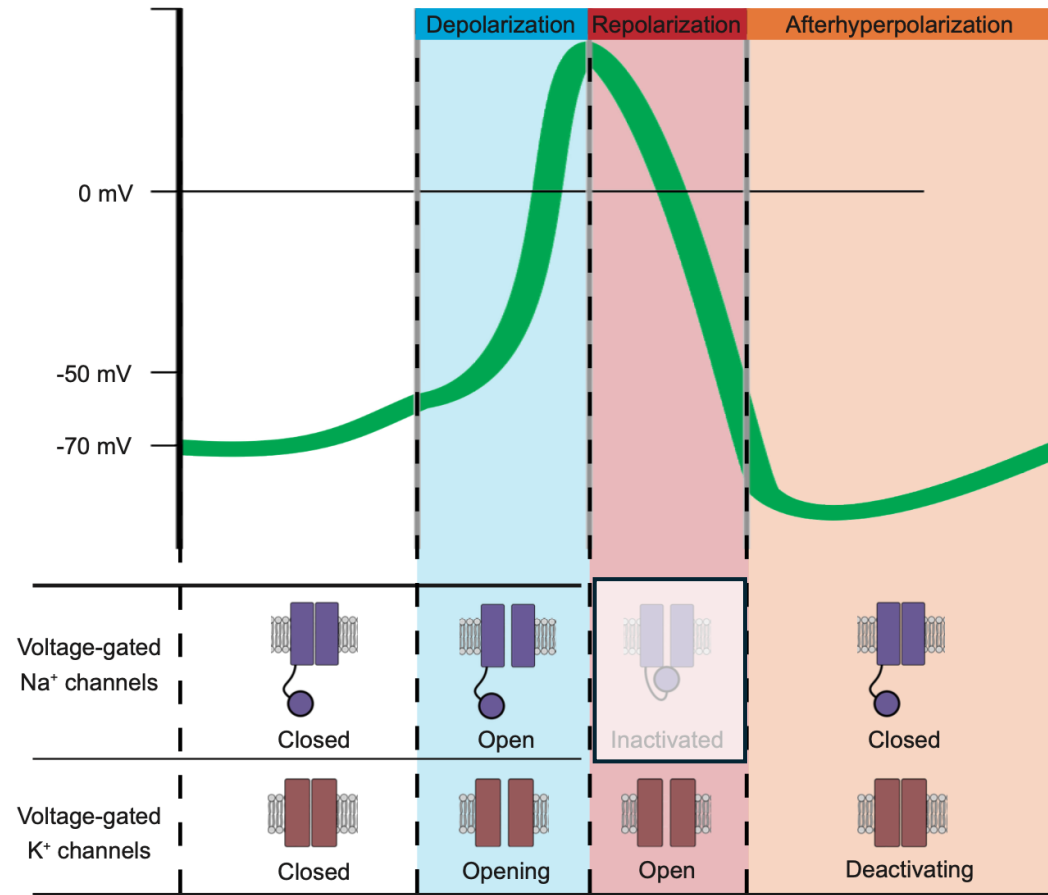
- Consider the individual ion that is moving
- When  $\text{Na}^+$  ions move into the cell, membrane potential shifts towards  $E_{\text{Na}}$  which is +55 mV (a depolarization)
- During repolarization, voltage-gated  $\text{K}^+$  channels open and  $V_m$  shifts towards  $E_{\text{K}}$ , which is -80 mV
- Consider GHK equation
  - As permeability to a given ion increases,  $V_m$  shifts towards equilibrium potential for that ion

# Refractory periods

- Absolute refractory period
  - Time window when second action potential cannot be fired
  - Lasts ~0.5 milliseconds (up to 1 millisecond)
  - Due to voltage-gated  $\text{Na}^+$  channels being inactivated (prevents  $\text{Na}^+$  from being able to pass any more inward excitatory current)
- Relative refractory period
  - Time window when it is more difficult to fire an action potential compared to resting condition
  - Only some voltage-gated  $\text{Na}^+$  channels have "reset" to closed (vs inactivated)
  - Plus, many voltage-gated  $\text{K}^+$  channels are still open, allowing  $\text{K}^+$  ions to move and neuron to be more negative
  - Lasts as long as afterhyperpolarization

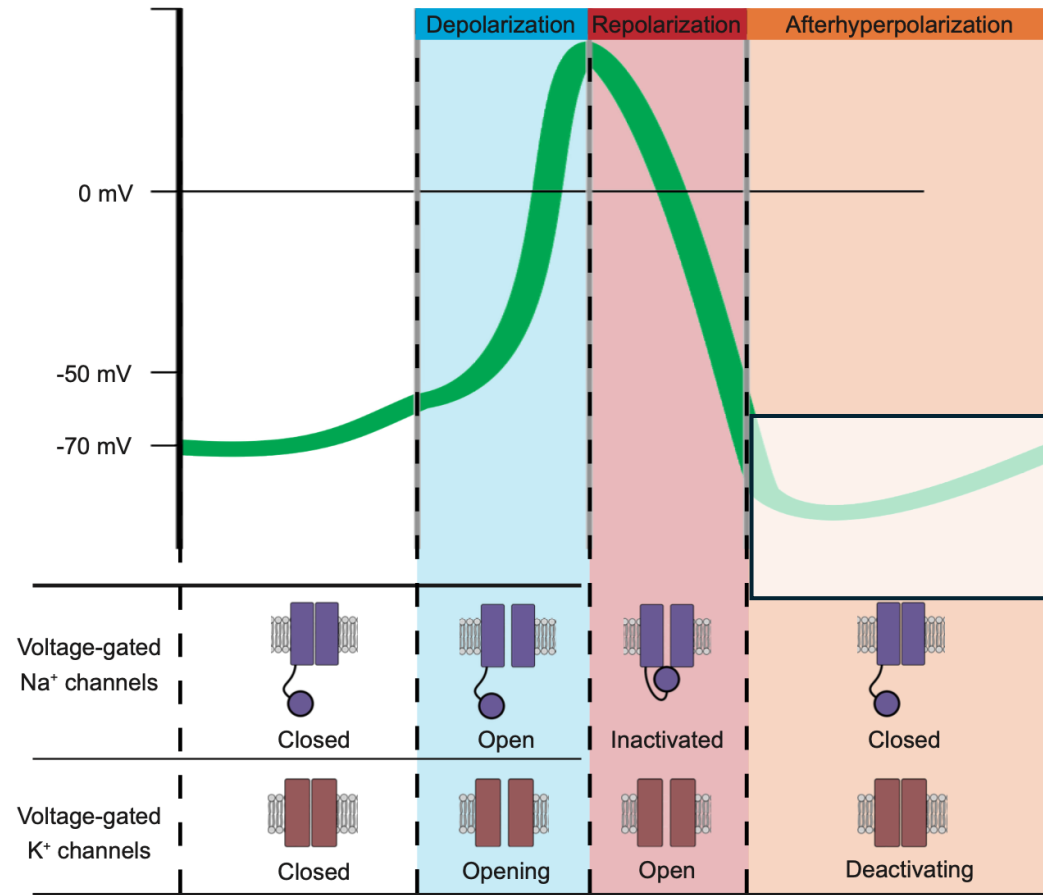


# Absolute refractory periods



**Figure 4.17** Voltage-gated ion channels open, inactivate, and deactivate at different times during the action potential.

# Relative refractory periods



The sooner after repolarization phase of the first action potential, the more difficult to reach threshold for a second action potential

**Figure 4.17** Voltage-gated ion channels open, inactivate, and deactivate at different times during the action potential.

# Movement of action potentials

- Been discussing what happens at a single section of a cell membrane
- But, for action potential to travel from hillock to terminal, change in  $V_m$  must physically move down length of axon
- Ability to travel is possible because  $\text{Na}^+$  entering cell are not restricted to cytoplasmic volume beneath ion channels
- $\text{Na}^+$  moves to area of lower concentration (chemical gradient) which is next section of membrane
- That section then becomes depolarized
- Next set of channels opens, allowing more  $\text{Na}^+$  influx
- Repeats down axon
- Chain reaction

# Action potentials are unidirectional

- $\text{Na}^+$  ions move down the concentration gradient (move forward)
- Previous patch of membrane is in absolute refractory period, making it impossible for action potential to travel backwards

# Analgesia and motor signaling

- Lidocaine is an inhibitory of voltage-gated  $\text{Na}^+$  channels
  - Blocking channels prevents action potentials from travelling up the afferent pathway, preventing incoming sensory inputs from area
- Similarly, outbound signals can be blocked
- Poison – efferent pathway is blocked, leading to paralysis
  - Pufferfish
    - Delicacy in Japan; dish is called fugu and can cause numbness of lips or even mild intoxication
    - Tetrodotoxin (TTX)
      - Produced by symbiotic bacteria (prevents predation)
      - Voltage-gated  $\text{Na}^+$  channel inhibitor
      - Prevents phrenic nerve from sending signals to move the diaphragm
      - People can die of respiratory failure in hours after exposure to 1 mg of TTX

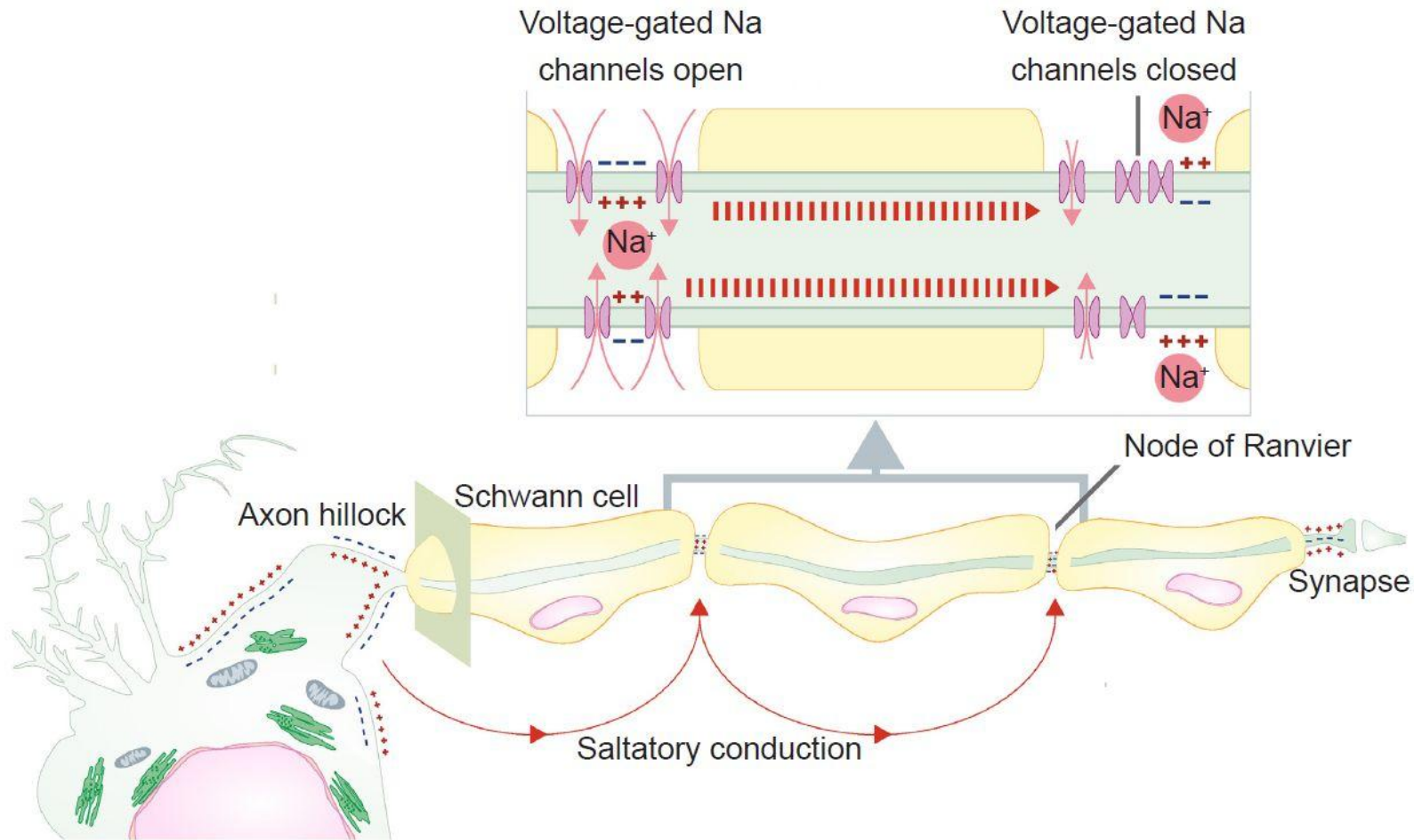


**Figure 4.20** Pufferfish and other species likely evolved a symbiotic relationship with bacteria that produce the deadly TTX to prevent predation.

# The role of myelin

- Increases conduction velocity, speed at which action potential travels
- Physically blocks leak  $K^+$  channels, preventing positive charges from exiting the cell
- Influx of  $Na^+$  is still required for signal to travel
- This influx happens at nodes of Ranvier (unmyelinated segments of axon)
- Nodes of Ranvier are dense with voltage-gated  $Na^+$  channels
- Saltatory conduction (Italian *saltare* = "jump")

# Saltatory conduction



**Figure 4.19** Movement of an action potential down a myelinated axon relies on saltatory conduction.